

Agenda: 8/10/15

- HW leader:
- Lesson 9
  - Log review
- Work on PS 9, 10
- \* Quiz 1 on Friday

Period 3

Ivan Malesko

Period 4

Mitchell Bryant

T/F The domain of the function  $g(z) = \frac{\sqrt{z+2}}{z-5}$  is  $\{z \in \mathbb{R} \mid z \geq -2\}$ .

## Logarithms Review

- Positive*
- Any number can be written as any positive base raised to some power

$$N = b^a$$

[Exponential form]

Define:

$$\log_b N = a$$

[logarithmic form]

) Two ways to write the same thing

Common logarithm:  $\log_{10} 42$  but write  $\log 42$

Natural logarithm:  $\log_e 42$  but write  $\ln 42$

Properties:

- $\log_b(a^x) = x \cdot \log_b a$
- $\log_b(b) = 1$
- $\log_b(a \cdot c) = \log_b a + \log_b c$
- $\log_b\left(\frac{a}{c}\right) = \log_b a - \log_b c$

Ex 9.10 Solve for  $x$ :  $\log_x(6x-9) = 2$

$$6x-9 = x^2 \quad [\text{Exponential form}]$$

$$x^2 - 6x + 9 = 0$$

$$(x-3)^2 = 0$$

$$x = 3$$

Check:

$$\log_3(6(3)-9)$$

$$= \log_3(9)$$

$$= \log_3(3^2) = 2 \quad \checkmark$$

• Domain for  $f(x) = \log_b(x)$  is all positive numbers.

• Domain for  $f(x) = b^x$  is  $\mathbb{R}$ .

Ex. Solve:  $\log_{1/3} P = 2 + \log_{1/3} 4$

$$\log_{1/3} \left(\frac{P}{4}\right) = 2$$

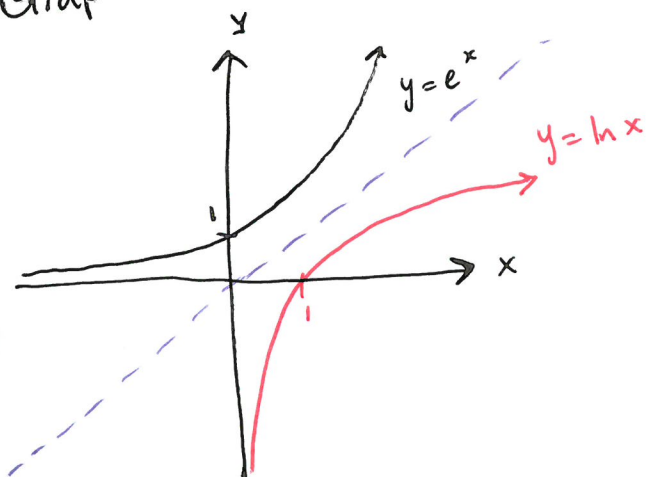
[Properties of logs]

$$\frac{P}{4} = \left(\frac{1}{3}\right)^2$$

[Exponential form]

$$P = \frac{4}{9}$$

Graphs:



Graph  $f(x) = \ln|x| = \begin{cases} \ln x & \text{if } x > 0 \\ \ln(-x) & \text{if } x < 0 \end{cases}$

