

Agenda: 9/15/15

HW leader:

Lesson 37

Chain Rule

★ Test 2 on Friday

Period 3

Lauren H.

Period 4

Ethan H.

Chain Rule (or Differentiation by u Substitution)

[Derivative for the composition of functions]

Idea: f and g are two differentiable functions

$$y = f(g(x))$$

let $u = g(x)$ then $y = f(u)$

$$\text{So } dy = f'(u) du$$

$$\text{Hence } \frac{dy}{dx} = f'(u) \frac{du}{dx}$$

$$\text{Chain Rule: } \frac{dy}{dx} = f'(g(x)) \cdot g'(x)$$

Ex. 37.1 If $f(x) = (x^2 + 2x)^{10}$ find $f'(x)$.

$$u = x^2 + 2x \quad \frac{du}{dx} = 2x + 2$$

$$f'(x) = f'(u) \cdot \frac{du}{dx} = 10(x^2 + 2x)^9 \cdot (2x + 2)$$

Ex 37.5 Find $\frac{dy}{dx}$ where $y = \sin^3 x = (\sin x)^3$

$$\begin{aligned} \frac{dy}{dx} &= 3 \sin^2 x \cdot \frac{d}{dx}(\sin(x)) \\ &= \boxed{3 \sin^2(x) \cdot \cos(x)} \end{aligned}$$

Ex 37.8 Find $\frac{dy}{dx}$ where $y = \ln|\cos x|$

$$\begin{aligned} \frac{dy}{dx} &= \frac{1}{\cos(x)} \cdot \frac{d}{dx}(\cos(x)) = \frac{-\sin(x)}{\cos(x)} = \boxed{-\tan(x)} \end{aligned}$$

x. Find $\frac{dw}{dz}$ where $w = \cos(e^{10z})$

$$\begin{aligned} \frac{dw}{dz} &= -\sin(e^{10z}) \cdot \frac{d}{dz}(e^{10z}) \\ &= -\sin(e^{10z}) \cdot e^{10z} \cdot \frac{d}{dz}(10z) \\ &= \boxed{-10e^{10z} \sin(e^{10z})} \end{aligned}$$