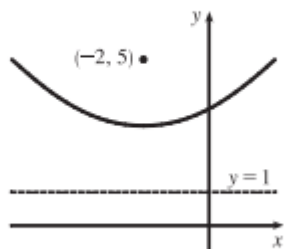
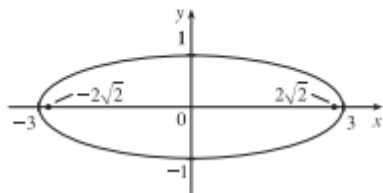


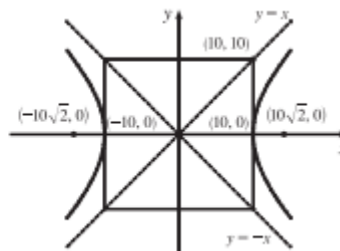
5.  $(x + 2)^2 = 8(y - 3)$ .  $4p = 8$ , so  $p = 2$ . The vertex is  $(-2, 3)$ , the focus is  $(-2, 5)$ , and the directrix is  $y = 1$ .



13.  $x^2 + 9y^2 = 9 \Leftrightarrow \frac{x^2}{9} + \frac{y^2}{1} = 1 \Rightarrow a = \sqrt{9} = 3$ ,  
 $b = \sqrt{1} = 1$ ,  $c = \sqrt{a^2 - b^2} = \sqrt{9 - 1} = \sqrt{8} = 2\sqrt{2}$ .  
 The ellipse is centered at  $(0, 0)$ , with vertices  $(\pm 3, 0)$ .  
 The foci are  $(\pm 2\sqrt{2}, 0)$ .



21.  $x^2 - y^2 = 100 \Leftrightarrow \frac{x^2}{100} - \frac{y^2}{100} = 1 \Rightarrow a = b = 10$ ,  
 $c = \sqrt{100 + 100} = 10\sqrt{2} \Rightarrow$  center  $(0, 0)$ , vertices  $(\pm 10, 0)$ ,  
 foci  $(\pm 10\sqrt{2}, 0)$ , asymptotes  $y = \pm \frac{10}{10}x = \pm x$



25.  $x^2 = y + 1 \Leftrightarrow x^2 = 1(y + 1)$ . This is an equation of a *parabola* with  $4p = 1$ , so  $p = \frac{1}{4}$ . The vertex is  $(0, -1)$  and the focus is  $(0, -\frac{3}{4})$ .
26.  $x^2 = y^2 + 1 \Leftrightarrow x^2 - y^2 = 1$ . This is an equation of a *hyperbola* with vertices  $(\pm 1, 0)$ . The foci are at  $(\pm\sqrt{1+1}, 0) = (\pm\sqrt{2}, 0)$ .
27.  $x^2 = 4y - 2y^2 \Leftrightarrow x^2 + 2y^2 - 4y = 0 \Leftrightarrow x^2 + 2(y^2 - 2y + 1) = 2 \Leftrightarrow x^2 + 2(y - 1)^2 = 2 \Leftrightarrow \frac{x^2}{2} + \frac{(y - 1)^2}{1} = 1$ . This is an equation of an *ellipse* with vertices at  $(\pm\sqrt{2}, 1)$ . The foci are at  $(\pm\sqrt{2-1}, 1) = (\pm 1, 1)$ .
28.  $y^2 - 8y = 6x - 16 \Leftrightarrow y^2 - 8y + 16 = 6x \Leftrightarrow (y - 4)^2 = 6x$ . This is an equation of a *parabola* with  $4p = 6$ , so  $p = \frac{3}{2}$ . The vertex is  $(0, 4)$  and the focus is  $(\frac{3}{2}, 4)$ .
29.  $y^2 + 2y = 4x^2 + 3 \Leftrightarrow y^2 + 2y + 1 = 4x^2 + 4 \Leftrightarrow (y + 1)^2 - 4x^2 = 4 \Leftrightarrow \frac{(y + 1)^2}{4} - x^2 = 1$ . This is an equation of a *hyperbola* with vertices  $(0, -1 \pm 2) = (0, 1)$  and  $(0, -3)$ . The foci are at  $(0, -1 \pm \sqrt{4+1}) = (0, -1 \pm \sqrt{5})$ .
30.  $4x^2 + 4x + y^2 = 0 \Leftrightarrow 4(x^2 + x + \frac{1}{4}) + y^2 = 1 \Leftrightarrow 4(x + \frac{1}{2})^2 + y^2 = 1 \Leftrightarrow \frac{(x + \frac{1}{2})^2}{1/4} + y^2 = 1$ . This is an equation of an *ellipse* with vertices  $(-\frac{1}{2}, 0 \pm 1) = (-\frac{1}{2}, \pm 1)$ . The foci are at  $(-\frac{1}{2}, 0 \pm \sqrt{1 - \frac{1}{4}}) = (-\frac{1}{2}, \pm\sqrt{3}/2)$ .