

# Section 16.1-16.3 Review

## • Section 16.1 - Vector fields

Vector field -

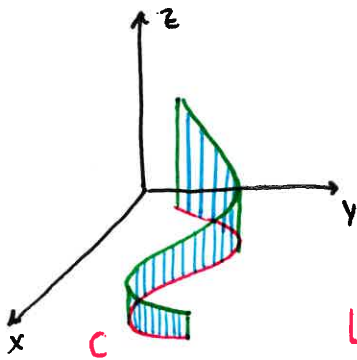
Ex.

Gradient Vector Field -

Definitions - a vector field  $\vec{F}$  is conservative if

Ex. Find a potential function for the conservative vector field  $\vec{F} = \langle \sin x, 2\cos y \rangle$

## • Section 16.2 - Line Integrals



Compute "area of ribbon" - with respect to arc length

Smooth  $C$ :  $\vec{r} = \langle x(t), y(t) \rangle$   $a \leq t \leq b$

$\Delta S =$

Area of rectangle =

Line Integral of  $f$  along  $C =$

Line Integrals with respect to  $x, y$ :  $\star$

$\star$

$$\int_C f(x, y) dx =$$

Notation:

$$\int_C f(x, y) dy =$$

Line Integral in Space:

Line Integral of Vector Fields:

## Section 16.1 - 16.3 Review

MVC

Ex. Find the work done by the force  $\vec{F} = \langle x^2, ye^x \rangle$  on a particle that moves along  $x = y^2 + 1$  from  $(1, 0)$  to  $(2, 1)$ .

### • Section 16.3 - The Fundamental Theorem for Line Integrals

$C$ -smooth curve given by  $\vec{r}(t)$ ,  $a \leq t \leq b$   
 $f$  differentiable with  $\nabla f$  continuous on  $C$

Path Independence:

Theorems: •

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•

Ex. Show  $\vec{F}$  is conservative, find  $f$  so  $\nabla f = \vec{F}$  and compute  $\int_C \vec{F} \cdot d\vec{r}$   
 $\vec{F} = \langle xy^2, x^2y + 1 \rangle$   $C: \vec{r}(t) = \langle \cos t, 2\sin t \rangle$   $0 \leq t \leq \pi/2$