

Agenda: 2/15/16

\* Handout WS 36

Geometric Progression (91)  
Probability of either (92)

Geometric Progression - a progression in which each succeeding term is formed by multiplying the previous term by a constant factor.

called the common ratio

Ex. 2, 4, 8, 16, 32, 64

$a_1$   $a_2$   $a_3$   $a_4$   $a_5$   $a_6$

2  $a_1 \cdot 2$   $a_1 \cdot 2^2$   $a_1 \cdot 2^3$   $a_1 \cdot 2^4$   $a_1 \cdot 2^5$  ...

$$a_n = a_1 \cdot 2^{(n-1)}$$

\* For any geometric progression with first term  $a_1$  and common ratio  $r$

then

$$a_n = a_1 \cdot r^{(n-1)}$$

x 91.1 Find the fifth term in a geometric sequence whose first term is -2 and common ratio is -3.

$$a_n = -2(-3)^{n-1}$$
 so  $a_5 = -2(-3)^{5-1} = -2(-3)^4 = -162$

Ex 91.3 Find two geometric means between 2 and  $\frac{1}{4}$ .

$a_1$   $a_2$   $a_3$   $a_4$   
2  $\frac{1}{2}$   $\frac{1}{4}$   
 $a_1$   $a_1 r$   $a_1 r^2$   $a_1 r^3$

$\Rightarrow \frac{1}{4} = 2r^3 \Rightarrow r = \frac{1}{2}$

$a_2 = 2 \cdot \frac{1}{2} = 1$   $a_3 = 2 \cdot \frac{1}{4} = \frac{1}{2}$

Probability of Either:

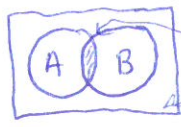
mutually exclusive events - when 1 event occurs the other event is excluded and cannot occur.

Ex. Flipping a coin heads or tails not both.

$P(A \text{ or } B) = P(A \cup B) = P(A) + P(B)$   $P(A \text{ and } B) = P(A \cap B) = 0$

Non-mutally exclusive events - overlap or intersection of A and B.

Venn Diagram



$P(A \cup B) = P(A) + P(B) - P(A \cap B)$

$P(A \cup B) = P(A) + P(B) + P(A \cap B) = \frac{4}{52} + \frac{26}{52} - \frac{2}{52} = \frac{7}{13}$

Ex 92.2

An urn contains 4 white balls and 3 black. 2 rough white, 1 rough black. P of rough or white.  $P = \frac{2}{7} + \frac{1}{7} - \frac{2}{7} = \frac{1}{7}$

Ex 92.1 A card is drawn from a full deck. Probability card is in ace or a black card.

Agenda: 2/16/16

Lesson 93

\* Quiz 11 tomorrow

Advanced Trig Identities  
Triangle Inequalities

$$\underline{\text{Ex}} \quad \frac{\cos B}{1 + \sin B} = \frac{1 - \sin B}{\cos B}$$

$$\text{RHS} = \frac{(1 - \sin B) \cos B}{\cos^2 B} \quad [\text{multiply } \frac{\cos B}{\cos B}]$$

$$= \frac{(1 - \sin B) \cos B}{1 - \sin^2 B} \quad [\text{Pythagorean}]$$

$$= \frac{(1 - \sin B) \cos B}{(1 - \sin B)(1 + \sin B)} \quad [\text{Difference of Squares}]$$

$$= \frac{\cos B}{1 + \sin B} = \text{LHS} \quad [\text{canceling}]$$

$$\underline{\text{Ex. Show}} \quad (x \tan \theta + y \sec \theta)^2 - (y \tan \theta + x \sec \theta)^2 = -x^2 + y^2$$

$$\text{LHS} = x^2 \tan^2 \theta + 2xy \tan \theta \sec \theta + y^2 \sec^2 \theta - (y^2 \tan^2 \theta + 2xy \tan \theta \sec \theta + x^2 \sec^2 \theta) \quad [\text{foil}]$$

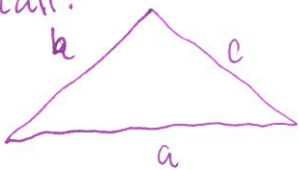
$$= \tan^2 \theta (x^2 - y^2) + \sec^2 \theta (y^2 - x^2) \quad [\text{factor + simplify}]$$

$$= \tan^2 \theta (x^2 - y^2) - \sec^2 \theta (x^2 - y^2) \quad [\text{factor}]$$

$$= (x^2 - y^2) (\tan^2 \theta - \sec^2 \theta) \quad [\text{factor}]$$

$$= -x^2 + y^2 = \text{RHS} \quad [\text{Pythagorean Identity}]$$

Recall:



$$\text{if } a^2 = b^2 + c^2 \Rightarrow \text{right triangle}$$

$$\text{if } a^2 > b^2 + c^2 \Rightarrow \text{obtuse triangle}$$

$$\text{if } a^2 < b^2 + c^2 \Rightarrow \text{acute triangle}$$

93.5 Classify the triangle whose sides are 4, 7, 5

$$4^2 + 5^2 = 16 + 25 = 41 < 49 \Rightarrow \boxed{\text{obtuse triangle}}$$

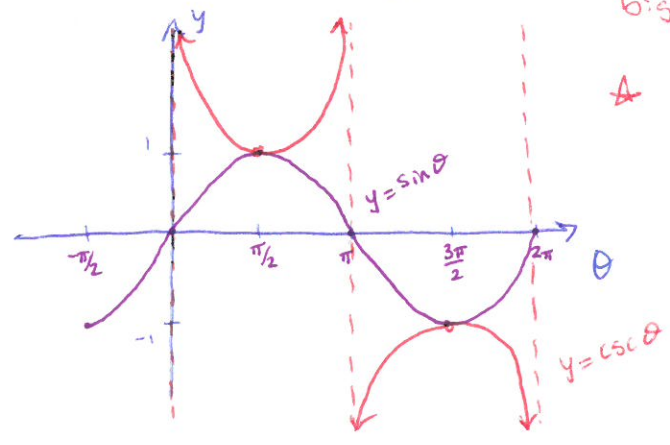
$$7^2 = 49$$

Agenda: 2/18/16  
Lesson 94 + 95

Graphs of  $\sec \theta$ ,  $\csc \theta$ ,  $\tan \theta$ ,  $\cot \theta$  (94)  
Advanced complex roots (95)

★ Quiz back after lesson  
★ Handout WS 37

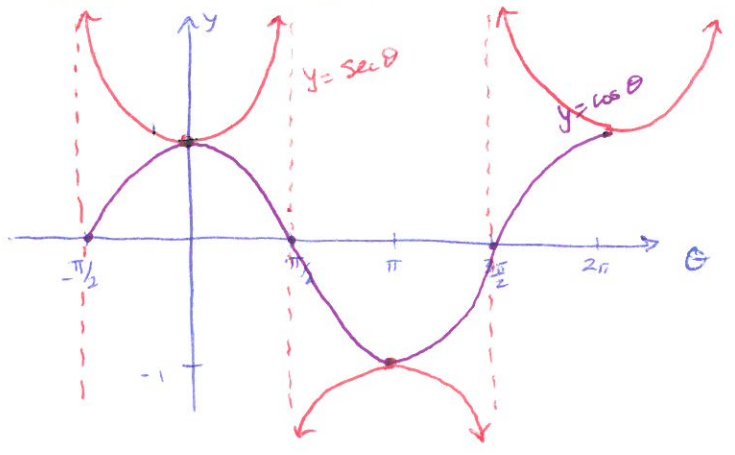
Recall:  $f(\theta) = \csc \theta = \frac{1}{\sin \theta}$



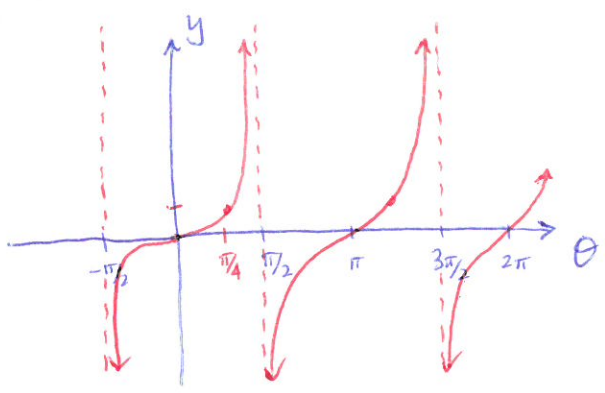
Small values  $\rightarrow$  big values  
big values  $\rightarrow$  small values

★ When  $\sin \theta = 0$   $\csc \theta$  is undefined

$f(\theta) = \sec \theta = \frac{1}{\cos \theta}$

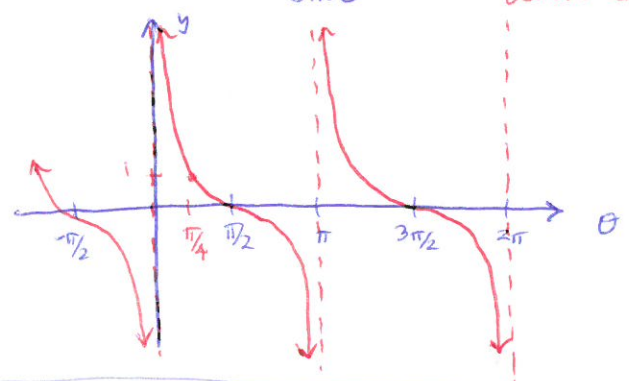


$f(\theta) = \tan \theta = \frac{\sin \theta}{\cos \theta}$



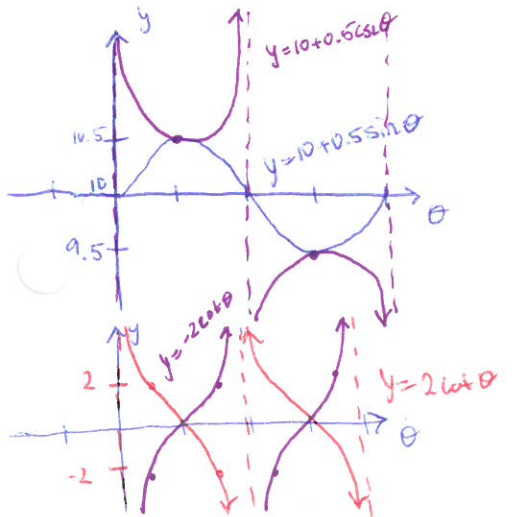
$f(\theta) = \cot \theta = \frac{\cos \theta}{\sin \theta}$

★  $\cot \theta$  is undefined when  $\sin \theta = 0$

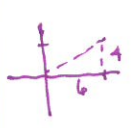


★  $\tan \theta$  is undefined when  $\cos \theta = 0$

Ex. Sketch  $y = 10 + 0.5 \csc \theta$  and  $y = -2 \cot \theta$



Ex. 95.1 Find the fourth roots of  $6 + 4i$  and express in polar form.



$r = \sqrt{52} \approx 7.21$      $\tan \theta = \frac{4}{6}$      $\theta = \arctan(\frac{4}{6}) \approx 33.69^\circ$

roots:  $(\sqrt{52} \text{ cis } 33.69^\circ)^{1/4} = 52^{1/8} \text{ cis } 8.4225^\circ$   
 $(\sqrt{52} \text{ cis } 399.69^\circ)^{1/4} = 52^{1/8} \text{ cis } 98.4225^\circ$   
 $(\sqrt{52} \text{ cis } 753.69^\circ)^{1/4} = 52^{1/8} \text{ cis } 188.4225^\circ$   
 $(\sqrt{52} \text{ cis } 1113.69^\circ)^{1/4} = 52^{1/8} \text{ cis } 278.4225^\circ$