

Answers to Worksheet 8 - Derivatives III

1) $y = 7s + 5$

2) $y = \frac{1}{8}x - \frac{5}{8}$

3) $y = 3x - \frac{13}{2}$

4) $\frac{d^3t}{dr^3} = -12$

5) $\frac{d^3y}{dt^3} = -120t^2$

6) $\frac{d^3g}{dx^3} = -300x^2 - 96x$

7) $\frac{dy}{dx} = \frac{9x^2}{2y}$

8) $\frac{dy}{dx} = \frac{3x}{5y}$

9) $\frac{dy}{dx} = \frac{-6xy^2 + 1}{6x^2y}$

10) $\frac{dy}{dx} = \frac{x^2}{2y^2}$

11) $\frac{dy}{dx} = \frac{3y^2 - 6x^2}{-2y - 6yx}$

12) $\frac{dy}{ds} = \frac{12}{\frac{1}{5s^5}}$

13) $\frac{dh}{ds} = -\frac{1}{\frac{2}{3s^3}}$

14) $\frac{dr}{dx} = \frac{10}{x^6}$

15)
$$\begin{aligned} \frac{dy}{dx} &= (-5 - 3x^{-2}) \cdot 25x^4 + (5x^5 - 1) \cdot 6x^{-3} \\ &= -125x^4 - 45x^2 - \frac{6}{x^3} \end{aligned}$$

16)
$$\begin{aligned} \frac{dt}{dr} &= \left(-2r^{\frac{1}{5}} + 5 \right) \cdot -4r + (-2r^2 - 1) \cdot -\frac{2}{5}r^{-\frac{4}{5}} \\ &= \frac{44r^{\frac{6}{5}}}{5} - 20r + \frac{2}{5r^{\frac{4}{5}}} \end{aligned}$$

17)
$$\begin{aligned} \frac{dg}{dx} &= (5 + 2x^{-4}) \cdot 2x + (x^2 - 4) \cdot -8x^{-5} \\ &= 10x - \frac{4}{x^3} + \frac{32}{x^5} \end{aligned}$$

18)
$$\begin{aligned} \frac{df}{dr} &= \left(-r^{\frac{3}{5}} + 4 \right) \cdot -15r^2 + (-5r^3 - 5) \cdot -\frac{3}{5}r^{-\frac{2}{5}} \\ &= 18r^{\frac{13}{5}} - 60r^2 + \frac{3}{r^{\frac{2}{5}}} \end{aligned}$$

19)
$$\begin{aligned} \frac{dy}{ds} &= \left(-4s^{\frac{1}{4}} + 2 \right) \cdot -8s + (-4s^2 + 4) \cdot -s^{-\frac{3}{4}} \\ &= 36s^{\frac{5}{4}} - 16s - \frac{4}{s^{\frac{3}{4}}} \end{aligned}$$