

## Answers to Worksheet 13 - Optimization

- 1)  $A$  = the total area of the two corrals  $x$  = the length of the non-adjacent sides of each corral

Function to maximize:  $A = 2x \cdot \frac{500 - 4x}{3}$  where  $0 < x < 125$

Dimensions of each corral:  $\frac{125}{2}$  ft (non-adjacent sides) by  $\frac{250}{3}$  ft (adjacent sides)

- 2)  $L$  = the total length of rope  $x$  = the horizontal distance from the short pole to the stake

Function to minimize:  $L = \sqrt{x^2 + 4^2} + \sqrt{(9 - x)^2 + 8^2}$  where  $0 \leq x \leq 9$

Stake should be placed: 3 ft from the short pole (or 6 ft from the long pole)

- 3)  $p$  = the profit per day  $x$  = the number of items manufactured per day

Function to maximize:  $p = x(130 - 0.05x) - (40x + 6000)$  where  $0 \leq x < \infty$

Optimal number of smartphones to manufacture per day: 900

- 4)  $V$  = the volume of the box  $x$  = the length of the sides of the squares

Function to maximize:  $V = (16 - 2x)(10 - 2x) \cdot x$  where  $0 < x < 5$

Sides of the squares: 2 in

- 5)  $A$  = the area of the rectangle  $x$  = half the base of the rectangle

Function to maximize:  $A = 2x\sqrt{5^2 - x^2}$  where  $0 < x < 5$

Area of largest rectangle: 25

- 6)  $d$  = the distance from point  $(5, 0)$  to a point on the curve  $x$  = the  $x$ -coordinate of a point on the curve

Function to minimize:  $d = \sqrt{(x - 5)^2 + (\sqrt{x})^2}$  where  $-\infty < x < \infty$

Point on the curve that is closest to the point  $(5, 0)$ :  $\left(\frac{9}{2}, \frac{3\sqrt{2}}{2}\right)$