

In-Class Together: Problems 1-6

① The radius of a circle is decreasing at a constant rate of 0.1 centimeter per second. In terms of the circumference C , what is the rate of change of the area of the circle, in square centimeters per second?

- (A) $-(0.2)\pi C$
(B) $-(0.1)C$
(C) $-\frac{(0.1)C}{2\pi}$
(D) $(0.1)^2 C$
(E) $(0.1)^2 \pi C$

② If the base b of a triangle is increasing at a rate of 3 inches per minute while its height h is decreasing at a rate of 3 inches per minute, which of the following must be true about the area A of the triangle?

- (A) A is always increasing.
(B) A is always decreasing.
(C) A is decreasing only when $b < h$.
(D) A is decreasing only when $b > h$.
(E) A remains constant.

③ If $\frac{dy}{dx} = 4y$ and if $y = 4$ when $x = 0$, then $y =$

- (A) $4e^{4x}$ (B) e^{4x} (C) $3 - e^{4x}$ (D) $4 + e^{4x}$ (E) $2x^2 - 4$

④ If $x^2 - xy = 10$, then when $x = 2$, $\frac{dy}{dx} =$

- (A) $-\frac{7}{2}$ (B) -2 (C) $\frac{2}{7}$ (D) $\frac{3}{2}$ (E) $\frac{7}{2}$
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⑤ If $x^2 - y^2 = 25$, what is the value of $\frac{d^2y}{dx^2}$ at the point $(4, 3)$?

- (A) $-\frac{25}{27}$ (B) $-\frac{7}{27}$ (C) $\frac{7}{27}$ (D) $\frac{3}{4}$ (E) $\frac{25}{27}$
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⑥ When the area in square units of an expanding circle is increasing twice as fast as its radius in linear units, the radius is

- (A) $\frac{1}{4\pi}$ (B) $\frac{1}{4}$ (C) $\frac{1}{\pi}$ (D) 1 (E) π
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In-Class: Problems 7-10

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- ⑦ If $\sin x = e^y$, $0 < x < \pi$, what is $\frac{dy}{dx}$ in terms of x ?
- (A) $-\tan x$ (B) $-\cot x$ (C) $\cot x$ (D) $\tan x$ (E) $\csc x$

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- ⑧ The radius r of a sphere is increasing at the uniform rate of 0.3 inches per second. At the instant when the surface area S becomes 100π square inches, what is the rate of increase, in cubic inches per second, in the volume V ? $\left(S = 4\pi r^2 \text{ and } V = \frac{4}{3}\pi r^3 \right)$
- (A) 10π (B) 12π (C) 22.5π (D) 25π (E) 30π

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- ⑨ If $f'(x) = -f(x)$ and $f(1) = 1$, then $f(x) =$
- (A) $\frac{1}{2}e^{-2x-2}$ (B) e^{-x-1} (C) e^{1-x} (D) e^{-x} (E) $-e^x$

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- ⑩ If $xy^2 + 2xy = 8$, then, at the point $(1, 2)$, y' is
- (A) $-\frac{5}{2}$ (B) $-\frac{4}{3}$ (C) -1 (D) $-\frac{1}{2}$ (E) 0
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Homework: Problems 11-18

- (11) The top of a 25-foot ladder is sliding down a vertical wall at a constant rate of 3 feet per minute. When the top of the ladder is 7 feet from the ground, what is the rate of change of the distance between the bottom of the ladder and the wall?

- (A) $-\frac{7}{8}$ feet per minute
 (B) $-\frac{7}{24}$ feet per minute
 (C) $\frac{7}{24}$ feet per minute
 (D) $\frac{7}{8}$ feet per minute
 (E) $\frac{21}{25}$ feet per minute

- (12) If $x^2 + xy + y^3 = 0$, then, in terms of x and y , $\frac{dy}{dx} =$

- (A) $-\frac{2x+y}{x+3y^2}$ (B) $-\frac{x+3y^2}{2x+y}$ (C) $\frac{-2x}{1+3y^2}$ (D) $\frac{-2x}{x+3y^2}$ (E) $-\frac{2x+y}{x+3y^2-1}$

- (13) The radius of a circle is increasing at a nonzero rate, and at a certain instant, the rate of increase in the area of the circle is numerically equal to the rate of increase in its circumference. At this instant, the radius of the circle is

- (A) $\frac{1}{\pi}$ (B) $\frac{1}{2}$ (C) $\frac{2}{\pi}$ (D) 1 (E) 2

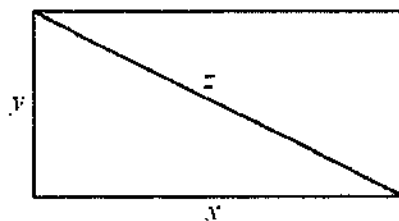
- (14) If $\frac{dy}{dt} = ky$ and k is a nonzero constant, then y could be

- (A) $2e^{ky}$ (B) $2e^{kt}$ (C) $e^{kt} + 3$ (D) $ky + 5$ (E) $\frac{1}{2}ky^2 + \frac{1}{2}$

- (15) The volume of a cone of radius r and height h is given by $V = \frac{1}{3}\pi r^2 h$. If the radius and the height both increase at a constant rate of $\frac{1}{2}$ centimeter per second, at what rate, in cubic centimeters per second, is the volume increasing when the height is 9 centimeters and the radius is 6 centimeters?
- (A) $\frac{1}{2}\pi$ (B) 10π (C) 24π (D) 54π (E) 108π

- (16) If $3x^2 + 2xy + y^2 = 2$, then the value of $\frac{dy}{dx}$ at $x=1$ is
- (A) -2 (B) 0 (C) 2 (D) 4 (E) not defined

- (17) If $\frac{dy}{dx} = 2y^2$ and if $y = -1$ when $x = 1$, then when $x = 2$, $y =$
- (A) $-\frac{2}{3}$ (B) $-\frac{1}{3}$ (C) 0 (D) $\frac{1}{3}$ (E) $\frac{2}{3}$



- (18) The sides of the rectangle above increase in such a way that $\frac{dz}{dt} = 1$ and $\frac{dx}{dt} = 3\frac{dy}{dt}$. At the instant when $x = 4$ and $y = 3$, what is the value of $\frac{dx}{dt}$?
- (A) $\frac{1}{3}$ (B) 1 (C) 2 (D) $\sqrt{5}$ (E) 5